

# Principles of wheel-rail interaction

***Sebastian Stichel, Railway Group  
KTH Royal Institute of Technology***

- 1. Wheel-rail guidance mechanisms**
  - a. Vehicle hunting
  - b. Vehicle curving
- 2. Creepages and creep forces**
- 3. The conflict between running in curves and running on straight track**
- 4. Designing a wheel-rail profile combination**



# Wheelset guidance mechanisms

**What is the main difference between the**

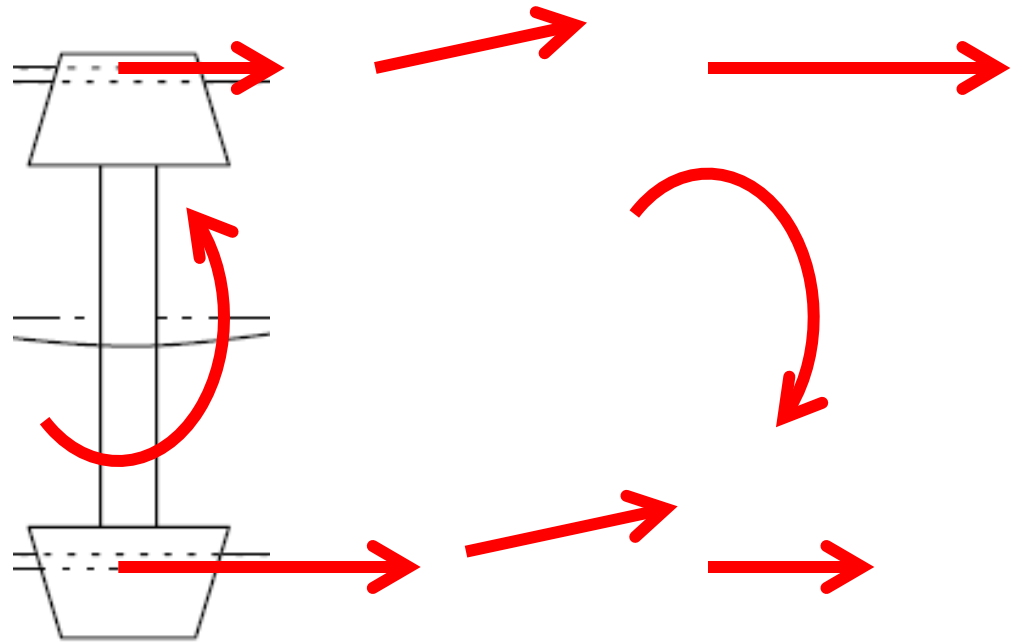
→ Two important Guidance mechanisms:

- Hunting motion on straight track
- Curving behaviour

**railway wheels have to have the same rotational speed**



# Wheelset hunting



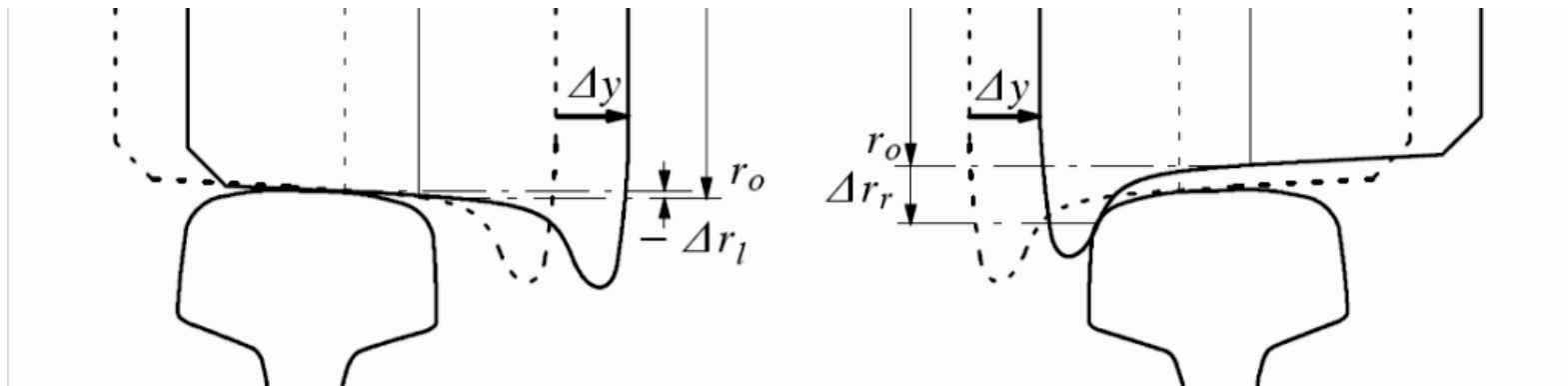
# Conicity and equivalent conicity

## Conicity $\lambda$ for a single wheel

$$\lambda = \frac{\Delta r}{\Delta y}$$

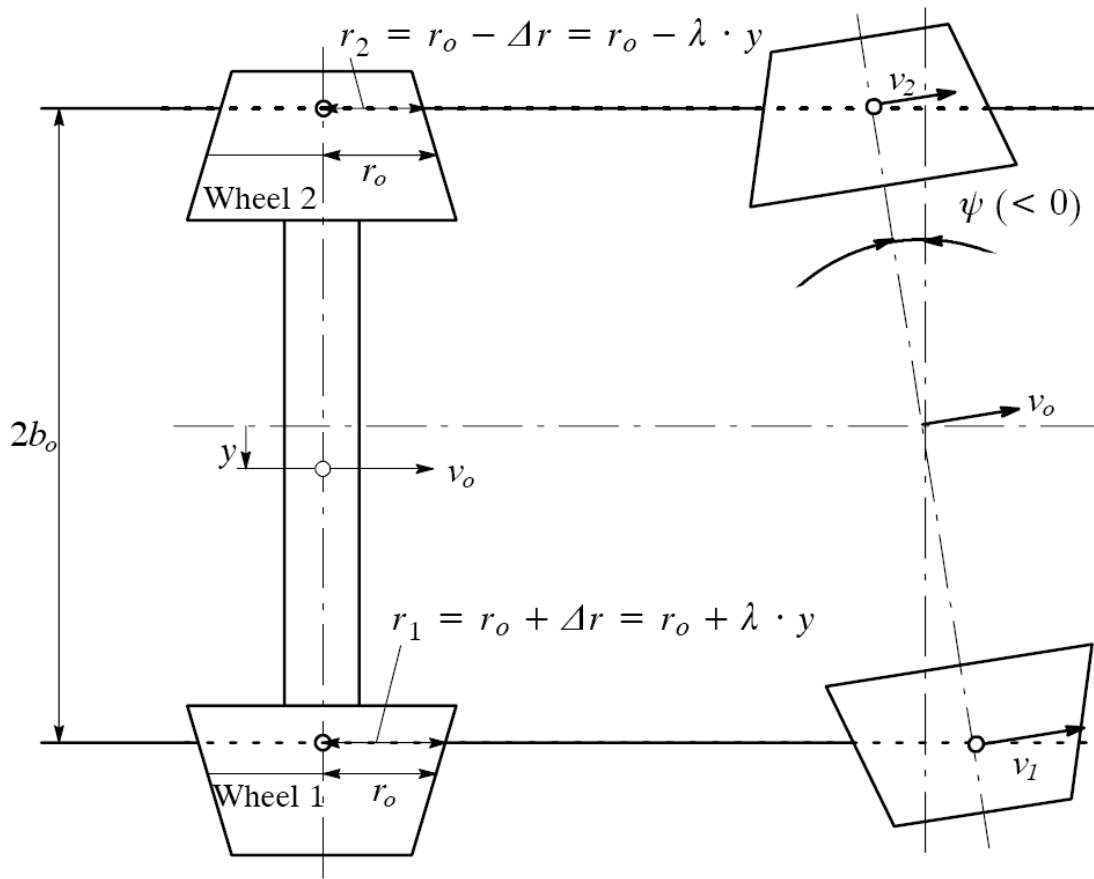
## Equivalent conicity $\lambda_{eq}$ for a wheelset

$$\lambda_{eq} = \frac{r_r - r_l}{2 \Delta y} = \frac{\Delta r_r - \Delta r_l}{2 \Delta y} \quad \text{for a defined lateral offset } \Delta y$$



# Klingel equation

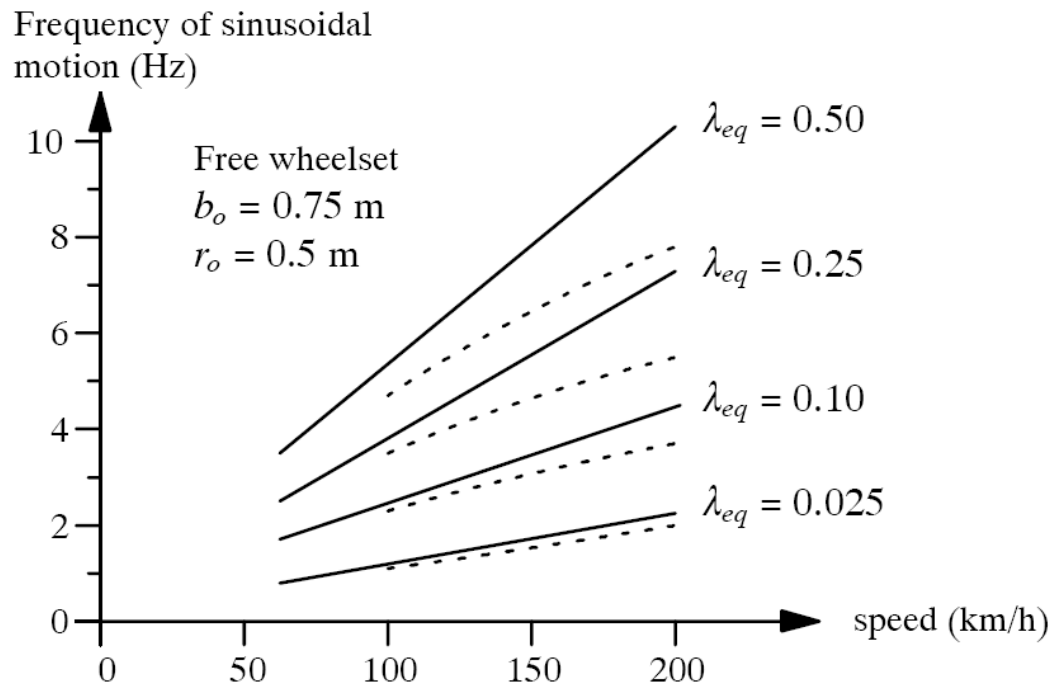
for a free wheelset with conical wheels:



$$L_o = 2\pi \sqrt{\frac{b_o r_o}{\lambda}}$$



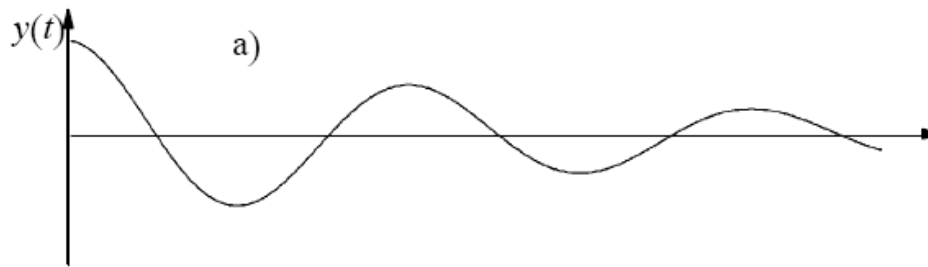
# Klingel equation



$$L_o = 2\pi \sqrt{\frac{b_o r_o}{\lambda}}$$

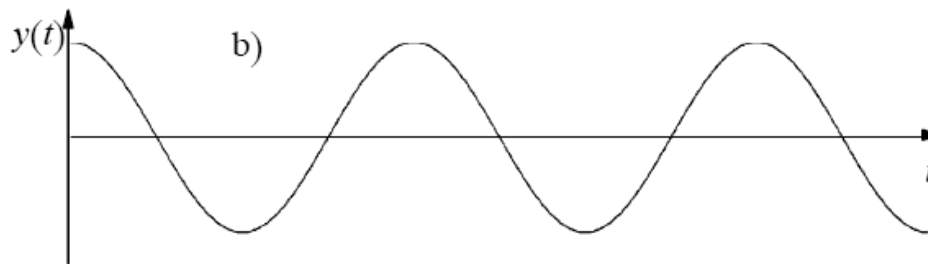


# Critical speed



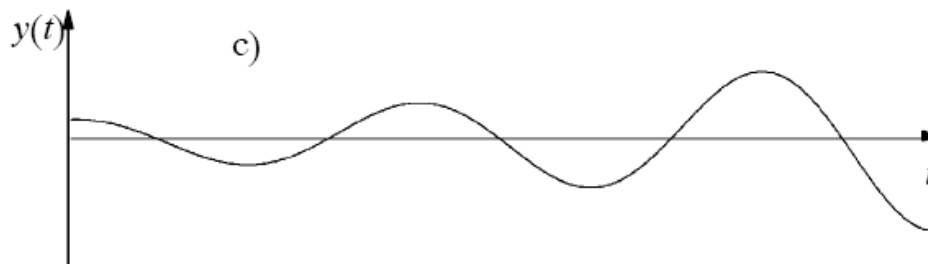
$v < \text{critical speed}$

damped oscillation,  
stable running



$v = \text{critical speed}$

undamped harmonic  
oscillation



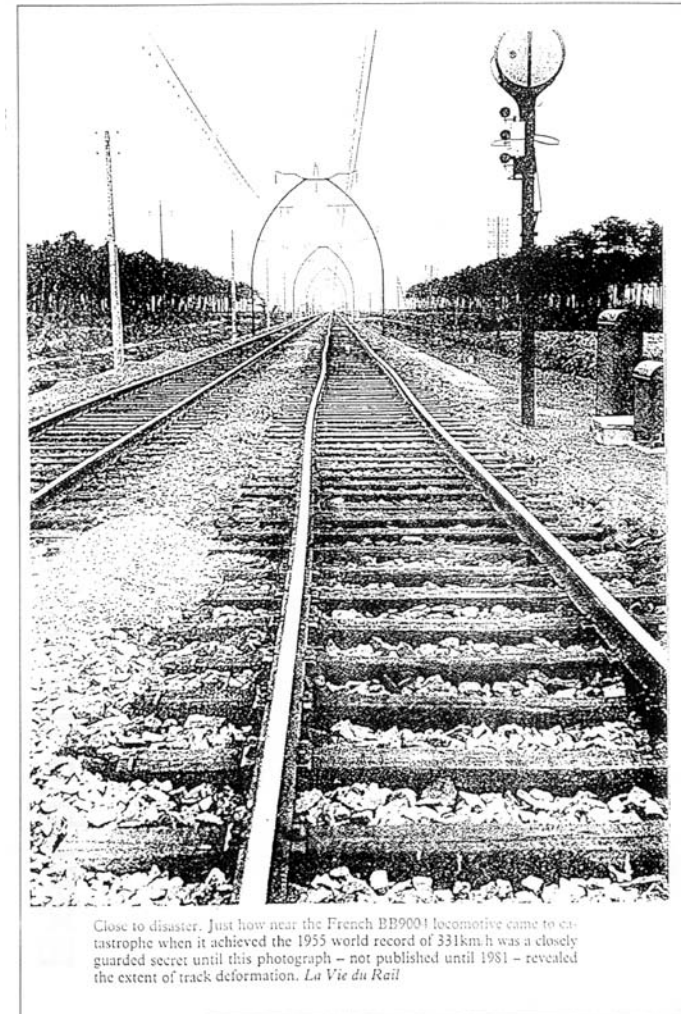
$v > \text{critical speed}$

unstable running



# Critical speed

**Track destroyed after severe bogie instability = "hunting"**

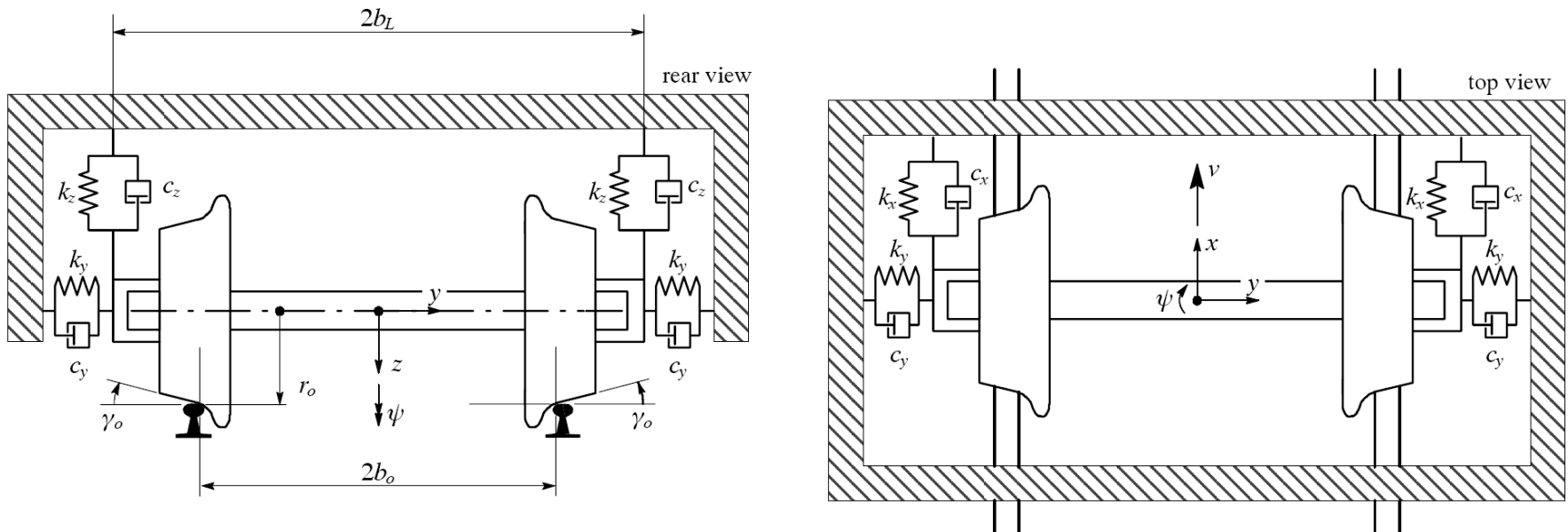


Close to disaster. Just how near the French BB9004 locomotive came to catastrophe when it achieved the 1955 world record of 331km/h was a closely guarded secret until this photograph – not published until 1981 – revealed the extent of track deformation. *La Vie du Rail*





# Simplified wheelset model



$r_o$  = nominal wheel radius

$k_x, k_y, k_z$  = stiffnesses wheelset/frame

$c_x, c_y, c_z$  = damper coefficients, dito



# Critical speed

$$\begin{aligned}
 & \begin{bmatrix} m & 0 \\ 0 & J \end{bmatrix} \begin{Bmatrix} \ddot{y} \\ \ddot{\psi} \end{Bmatrix} + \begin{bmatrix} 2c_y & 0 \\ 0 & 2b_L^2 c_x \end{bmatrix} \begin{Bmatrix} \dot{y} \\ \dot{\psi} \end{Bmatrix} + \frac{1}{v} \begin{bmatrix} 2\kappa_{22} & 2\kappa_{23} \\ 0 & 2b_o^2 \kappa_{11} \end{bmatrix} \begin{Bmatrix} \dot{y} \\ \dot{\psi} \end{Bmatrix} + \\
 & + \begin{bmatrix} 2k_y + 2\kappa \left( Q_o - \frac{\kappa_{23}}{r_o} \right) & -2\kappa_{22} \\ \frac{2b_o \kappa_{11} \lambda_{eq,a}}{r_o} & 2b_L^2 k_x \end{bmatrix} \begin{Bmatrix} y \\ \psi \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}
 \end{aligned}$$



# What influences critical speed?

- Conicity
- Longitudinal stiffness bogie  $\leftrightarrow$  wheelset
- Bogie wheelset distance
- Wheelset mass
- Bogie mass / inertia moment



# Equivalent conicity according to UIC 518 / EN14363

$\lambda_{eq} \leq 0.50$  for speeds up to 140 km/h

$\lambda_{eq} \leq 0.40$  for speeds above 140 km/h and up to 200 km/h

$\lambda_{eq} \leq 0.35$  for speeds above 200 km/h and up to 230 km/h

$\lambda_{eq} \leq 0.30$  for speeds above 230 km/h and up to 250 km/h

$\lambda_{eq} \leq 0.25$  for speeds above 250 km/h and up to 280 km/h

$\lambda_{eq} \leq 0.15$  for speeds above 280 km/h and up to 350 km/h

**High conicity** is usually the "**worst case**".

(Sometimes low conicity may also be a severe case.)



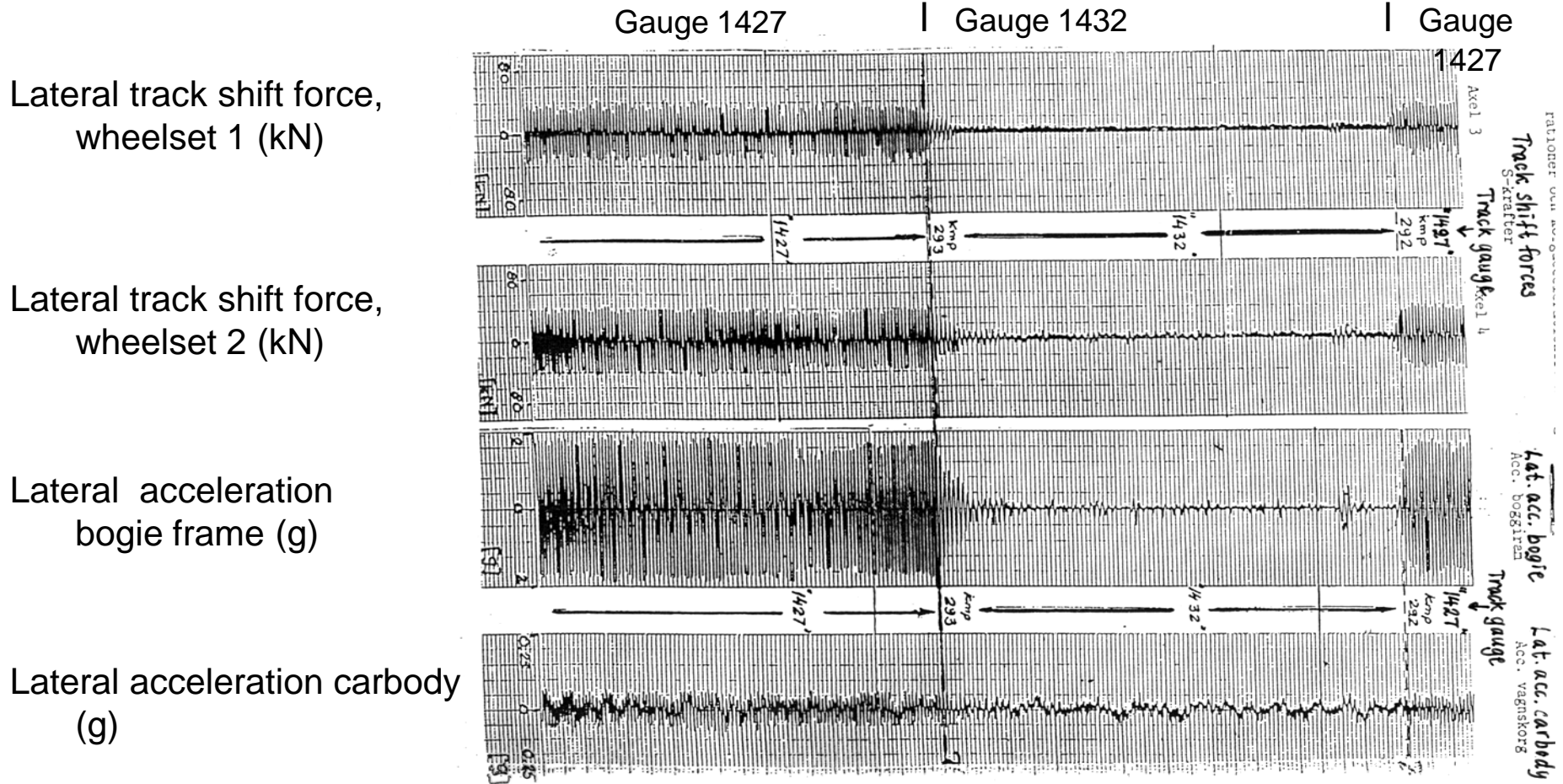
# Influences on equivalent conicity

**High conicity** may be produced by

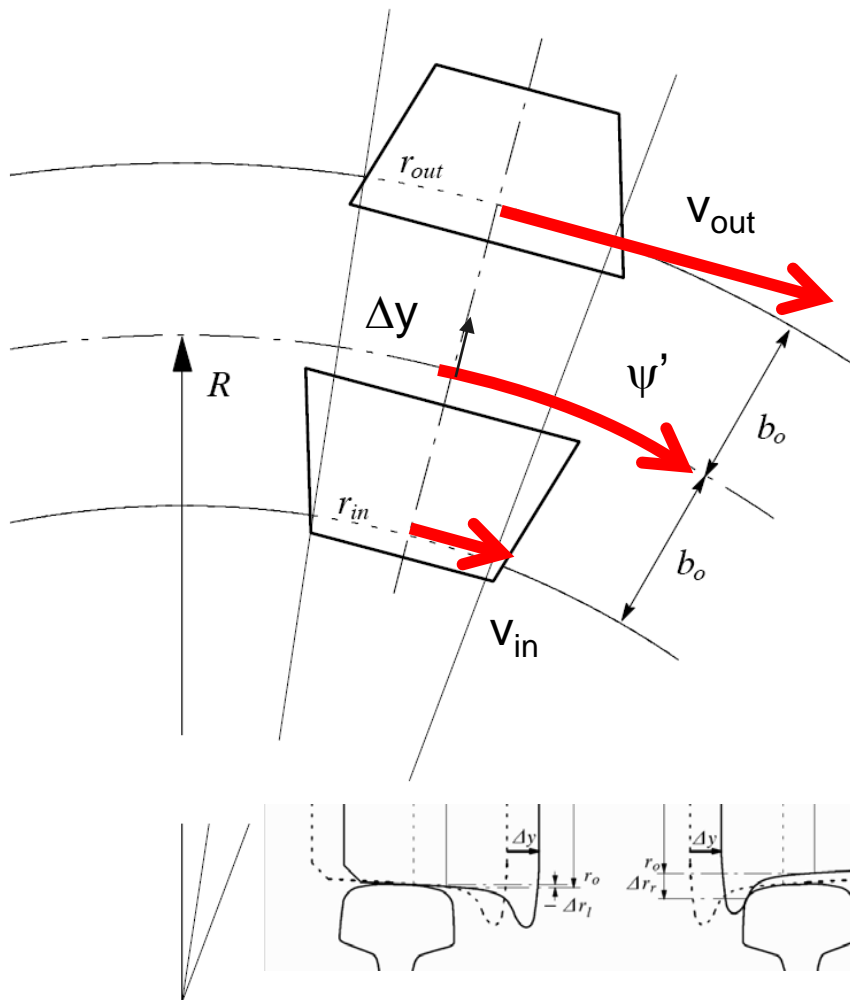
- Tight track gauge
- Low rail inclination
- Flat top of rail (=worn on tangent track)
- Wide wheel gauge
- Thick flanges
- Hollow wheel profiles (=worn)



# Example: Instability on narrow gauge



# Vehicle curving



For ideal curving:

$$\frac{r_{out}}{r_{in}} = \frac{R + b_o}{R - b_o}$$

which turns to

$$r_{out} - r_{in} = 2r_o \frac{b_o}{R}$$

Of advantage is:

- **High conicity**
- **High w/r friction**
- **Wheelset free** to take radial position





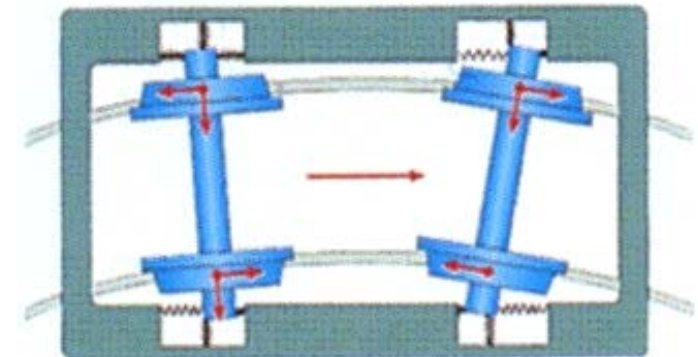
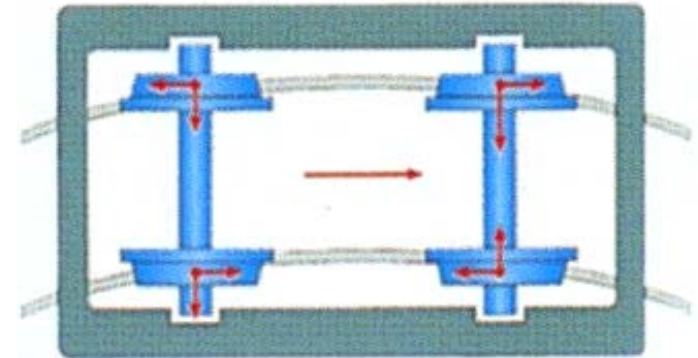
# ... it is not that simple

Wheelsets are usually more or less constrained in a frame.

Forces are needed to turn around the wheelset.

With very "stiff" constraints the wheelset is never able to radial self-steering.

With "flexible" or "soft" constraints the wheelset is more or less able to steer radially depending on friction, curve radius, etc.



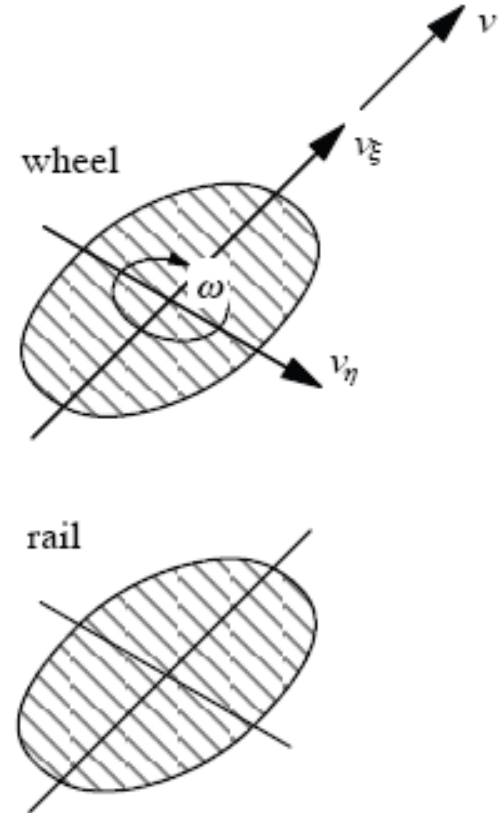


# Friction and creep

**Friction forces** are usually acting in the wheel-rail interface.

Some "**sliding**" is necessary to generate these friction forces.

Sliding under simultaneous rolling is called creep.



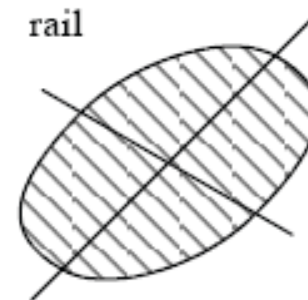
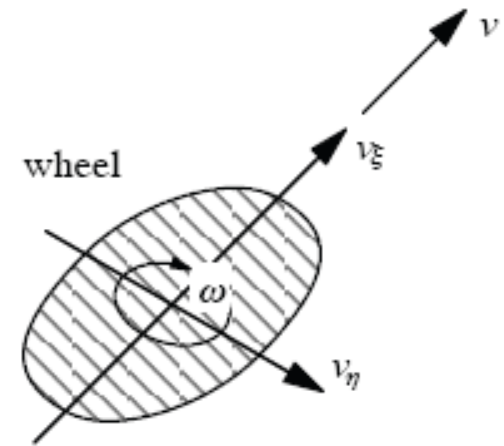
# Creep -Definitions

$V_{\xi}$  = longitudinal sliding speed wheel-rail (m/s)

$V_{\eta}$  = lateral sliding speed wheel-rail (m/s)

$\omega$  = rotational sliding speed (spin) wheel-rail (rad/s)

$V$  = forward speed (m/s)



*longitudinal creep*       $v_{\xi} = \frac{v_{\xi}}{v}$

*lateral creep*       $v_{\eta} = \frac{v_{\eta}}{v}$

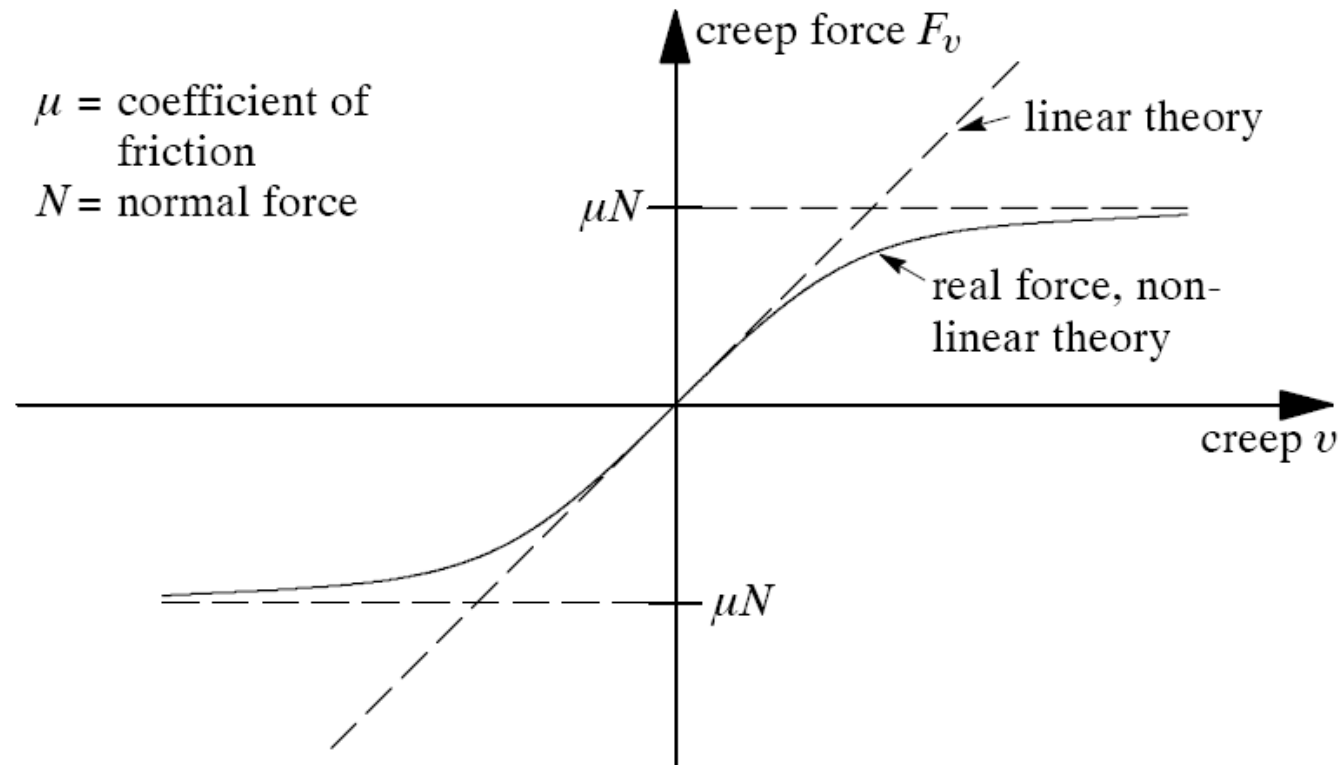
*spin creep*       $\phi = \frac{\omega}{v}$

total creep

$$v = \sqrt{v_{\xi}^2 + v_{\eta}^2}$$

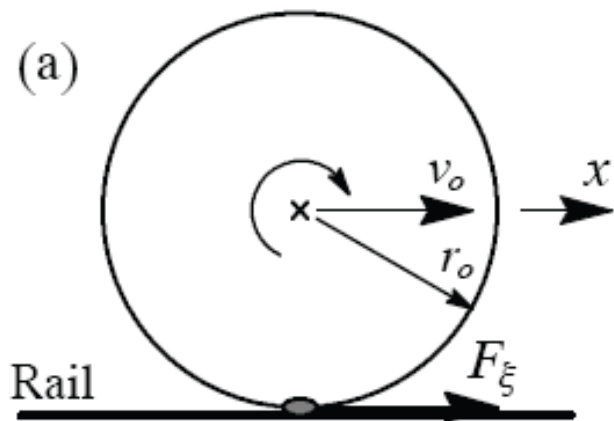


# Creep → Creep forces



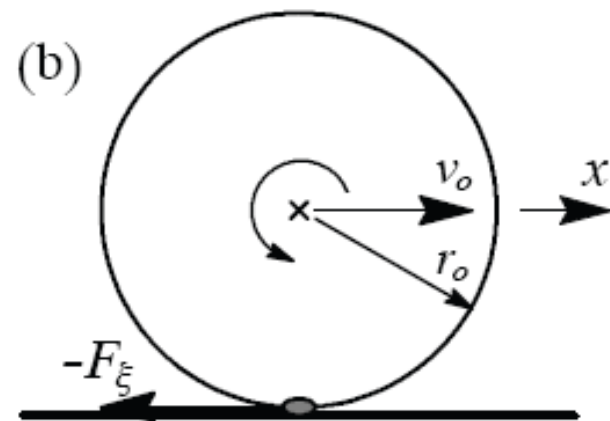
# Creep and creep forces

## Example 1: Wheel in driving or braking



$$v_{\xi} < 0$$

$$F_{\xi} > 0 \quad (\text{Driving})$$



$$v_{\xi} > 0$$

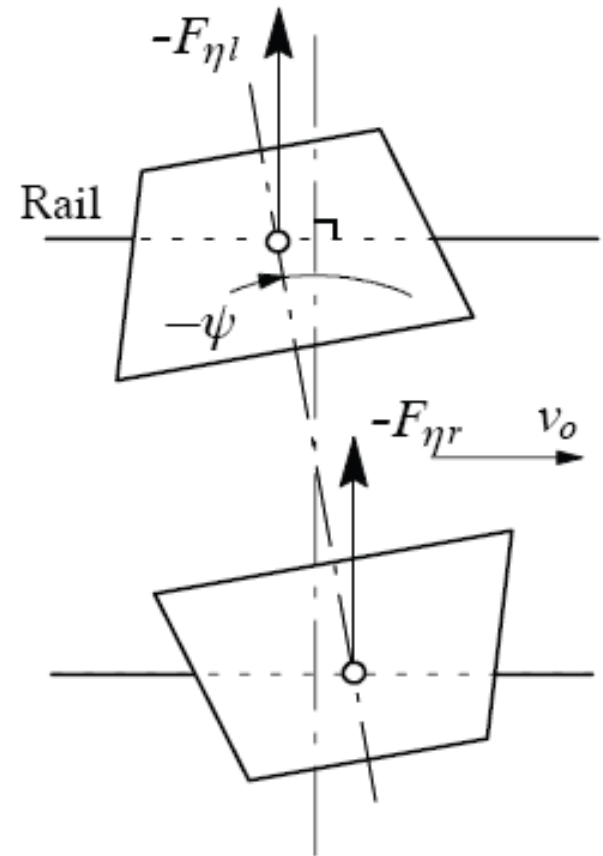
$$F_{\xi} < 0 \quad (\text{Braking})$$



# Creep and creep forces

## Example 2: Wheel angle of attack

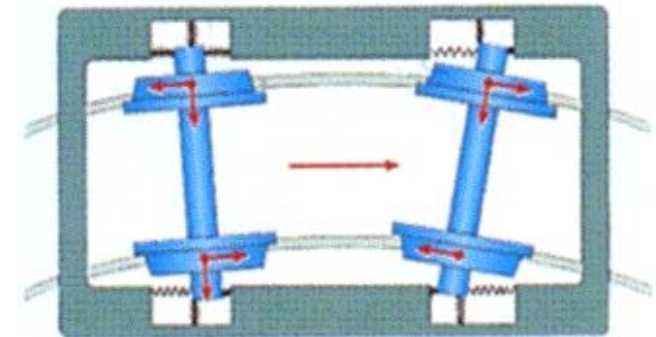
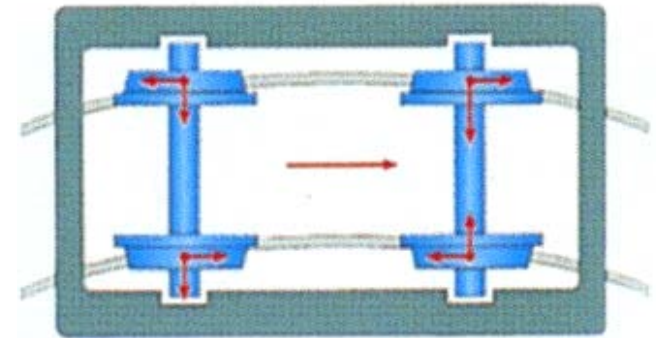
- There is a continuous "sliding" (creep) in lateral direction; thus a steady lateral creep force is generated



# Vehicle curving again

How will the wheelset behave in reality?

- Radial steering or not?
- Which forces?



# Vehicle curving

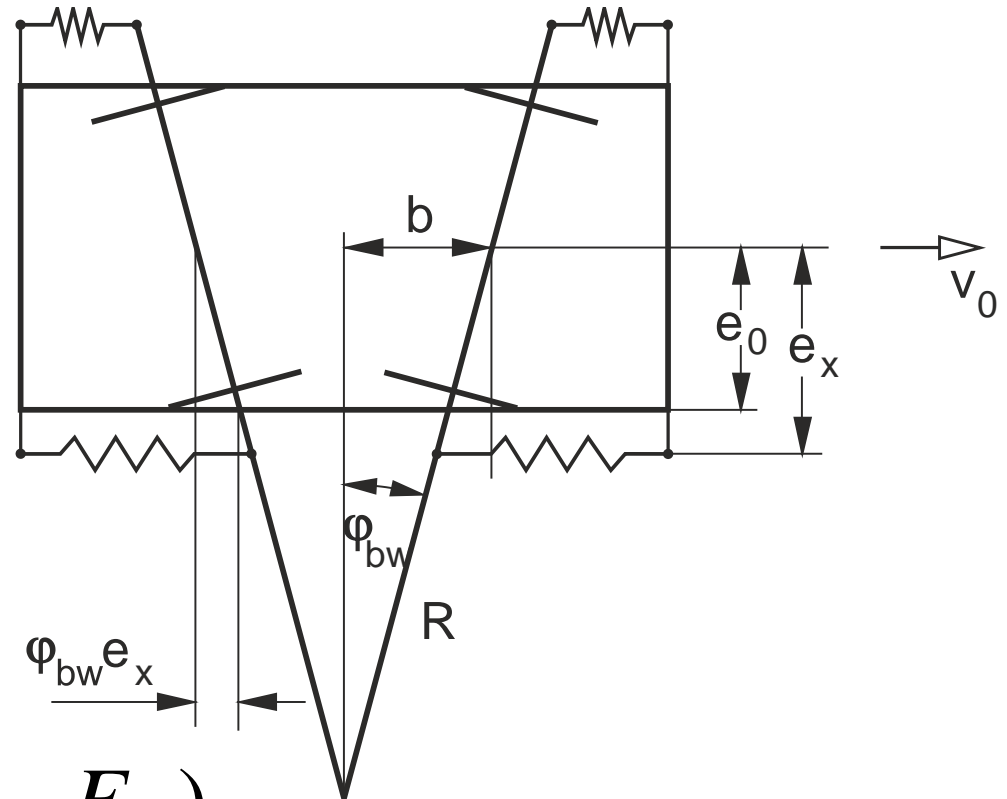
Force moment from longitudinal suspension:

$$2e_x^2 \cdot k_x \varphi_{bw} = ?$$

Balanced by

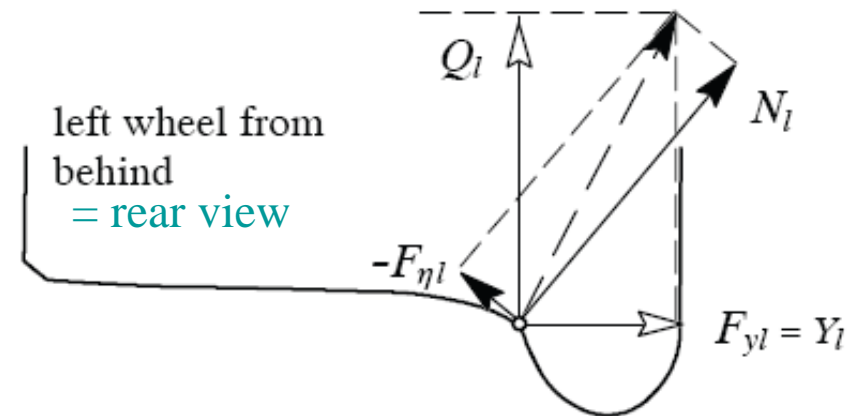
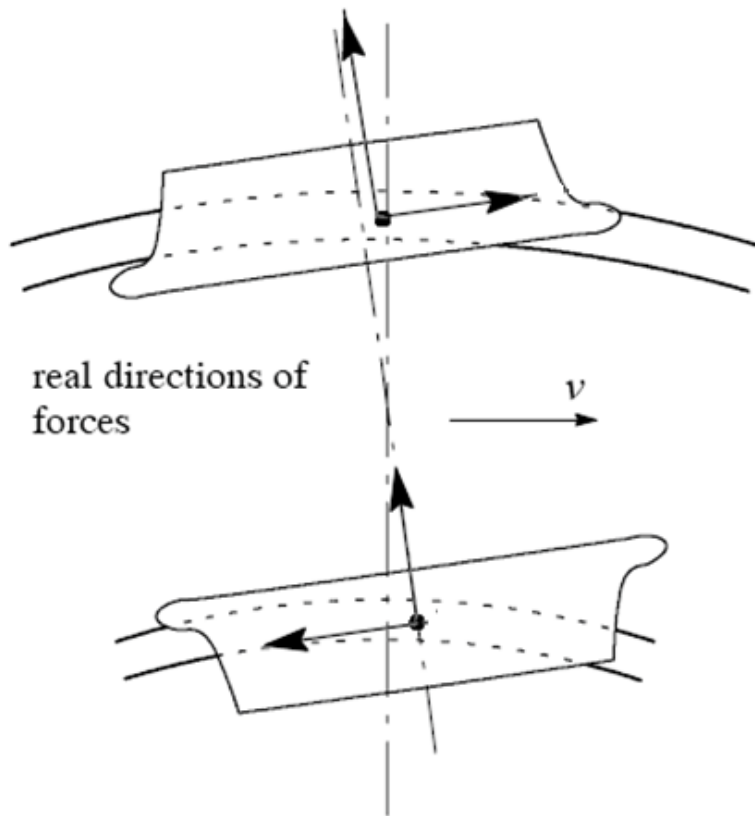
$$2e_x^2 \cdot k_x \varphi_{bw} = e_0 (F_{\xi l} - F_{\xi r})$$

... the longitudinal creep forces



# Forces on wheelset

Case 1: One-point contact on outer wheel  
= usually good; develop forces for radial steering

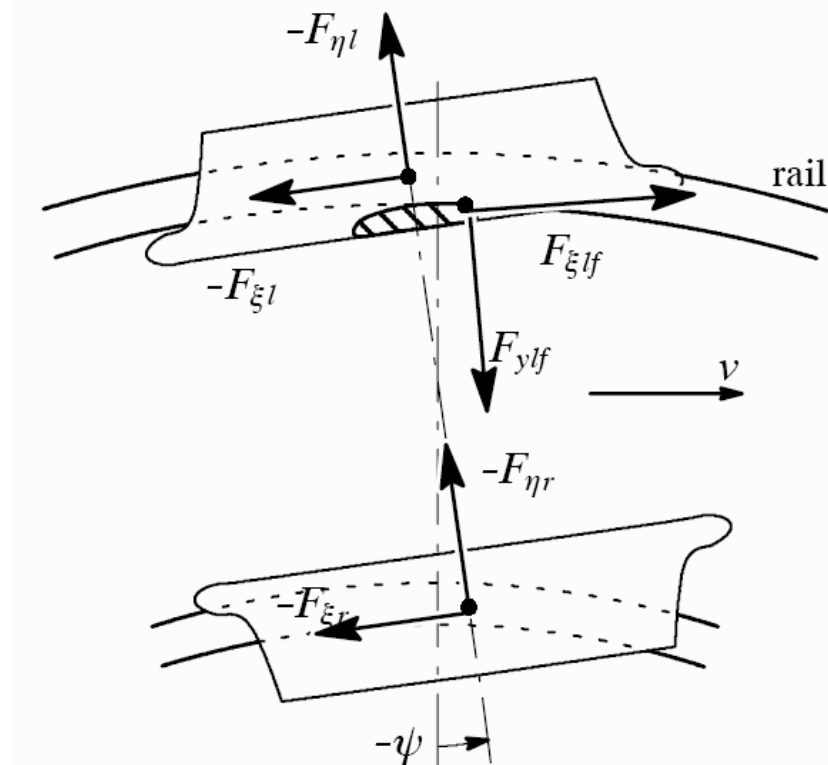




# Forces on wheelset

Case 2: Two point contact on outer wheel.

Will usually not develop forces for radial steering

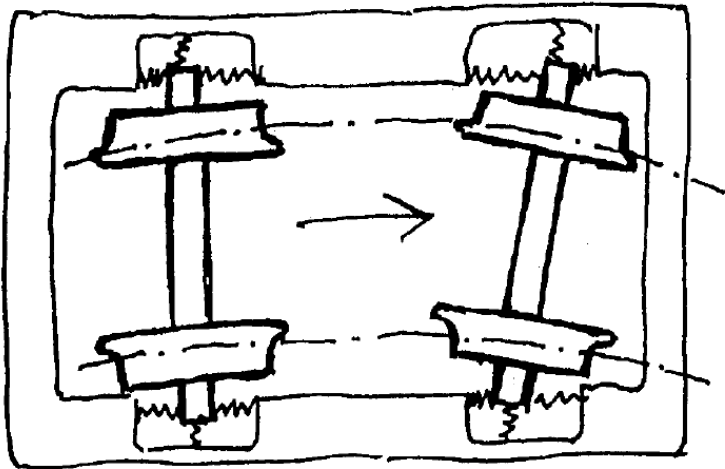


(a) Top view of wheelset



# Examples of forces in a curve

## Flexible wheelset guidance (F)



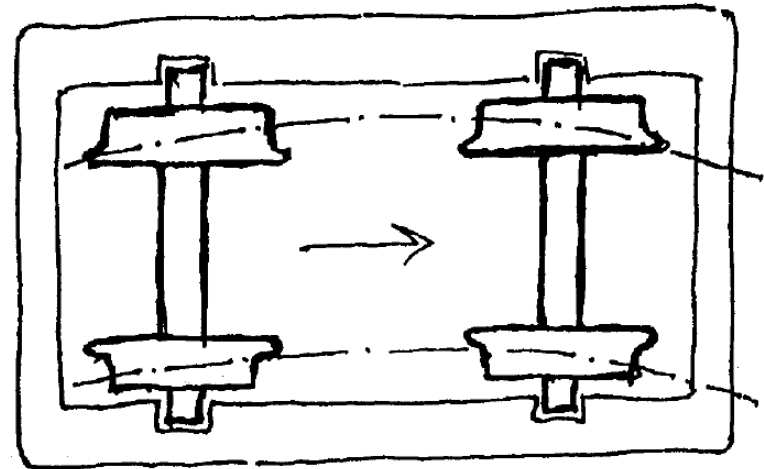
$k_x = 4\,000 \text{ kN/m}$  per axle box

$k_y = 1\,000 \text{ kN/m}$  per axle box

## Stiff wheelset guidance (S)

$k_x = 40\,000 \text{ kN/m}$  per axle box

$k_y = 15\,000 \text{ kN/m}$  per axle box

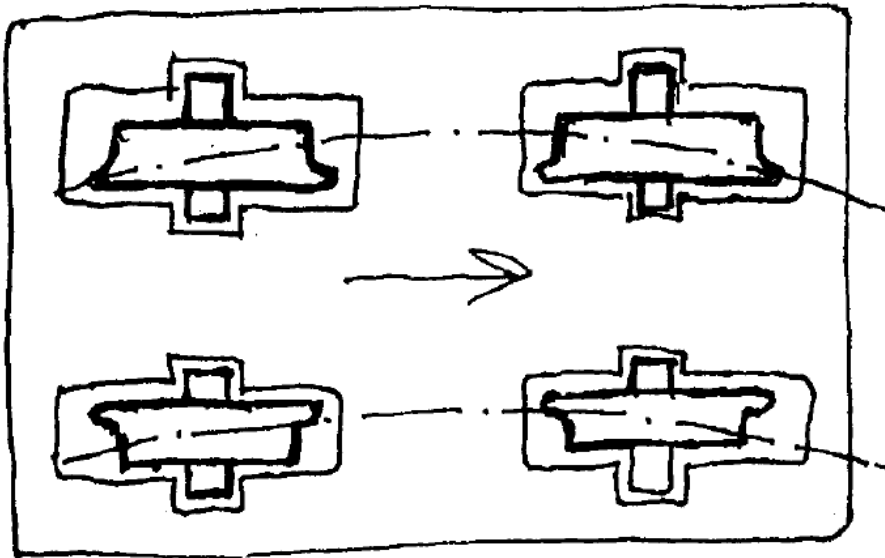


# Examples of forces in a curve

Stiff wheelset guidance, independently rotating wheels (SI)

$k_x = 40\,000 \text{ kN/m}$  per axle box

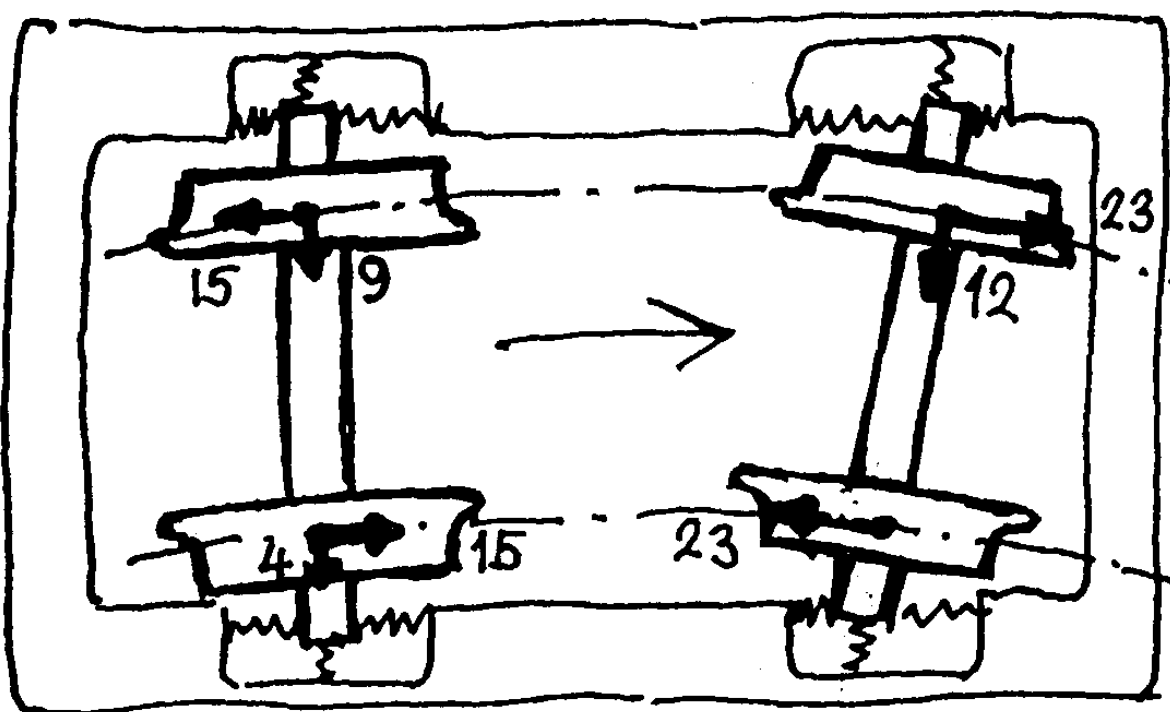
$k_y = 15\,000 \text{ kN/m}$  per axle box



# Examples of forces in a curve

$R=400$  m,  $h_t=145$  mm,  $v=90$  km/h: Soft bogie

Forces in kN, AoA  $\alpha$ , roll radius increase  $\Delta r$ , Y/Q, energy diss. E



$$\Delta r = 4 \text{ mm}$$

$$Y/Q = 0.10$$

$$E = 145 \text{ Nm/m}$$

$$\Delta r \approx 0$$

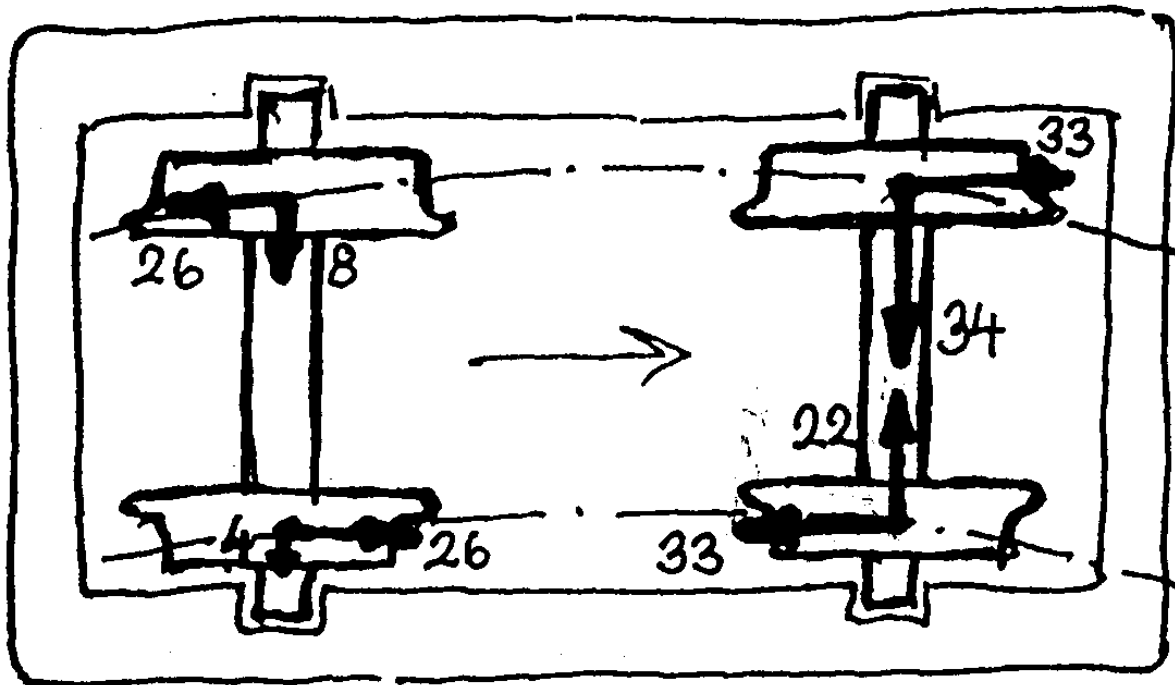
$$E = 45 \text{ Nm/m}$$



# Examples of forces in a curve

$R=400$  m,  $h_t=145$  mm,  $v=90$  km/h: Stiff bogie

Forces in kN, AoA  $\alpha$ , roll radius increase  $\Delta r$ , Y/Q, energy diss. E



$\Delta r = 10$  mm

Y/Q = 0.29

E = 655 Nm/m

$\Delta r = -0.5$  mm

E = 436 Nm/m

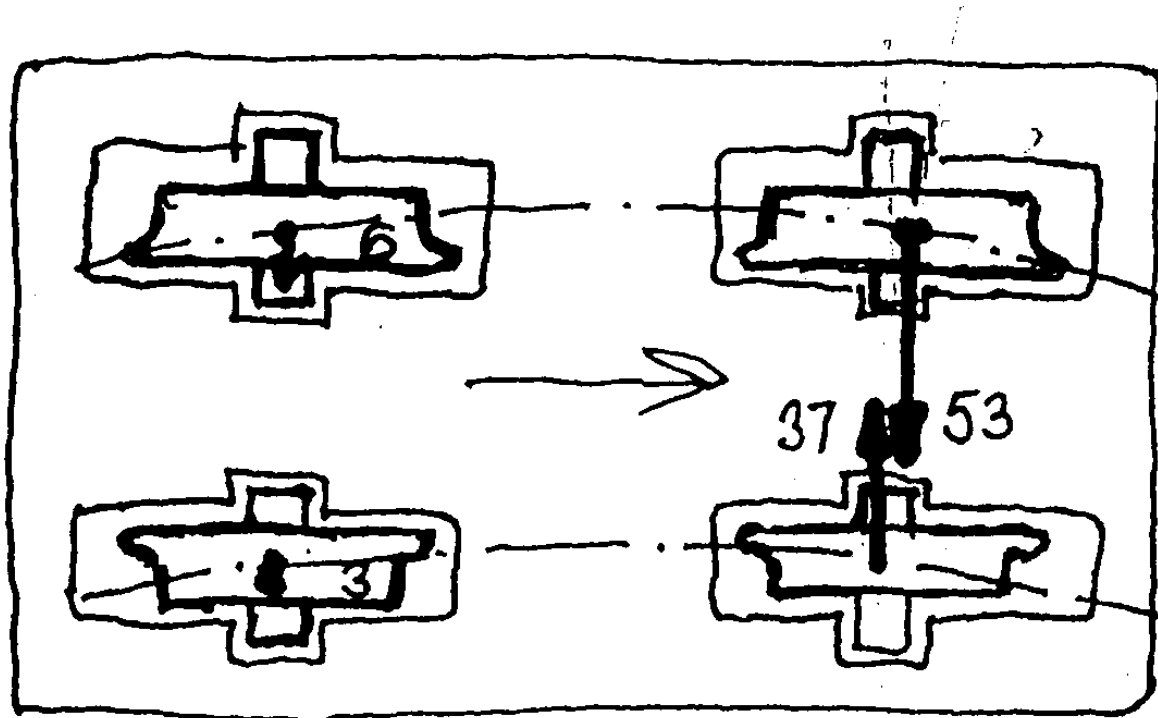
$\alpha = -0.5$  mrad

$\alpha = 6$  mrad



# Examples of forces in a curve

$R=400$  m,  $h_t=145$  mm,  $v=90$  km/h: Stiff-indep  
Forces in kN, AoA  $\alpha$ , roll radius increase  $\Delta r$ , Y/Q, energy diss.  $E$



$$\Delta r = 15 \text{ mm}$$

$$Y/Q = 0.45$$

$$E = 606 \text{ Nm/m}$$

$$\Delta r = -1 \text{ mm}$$

$$E = 266 \text{ Nm/m}$$

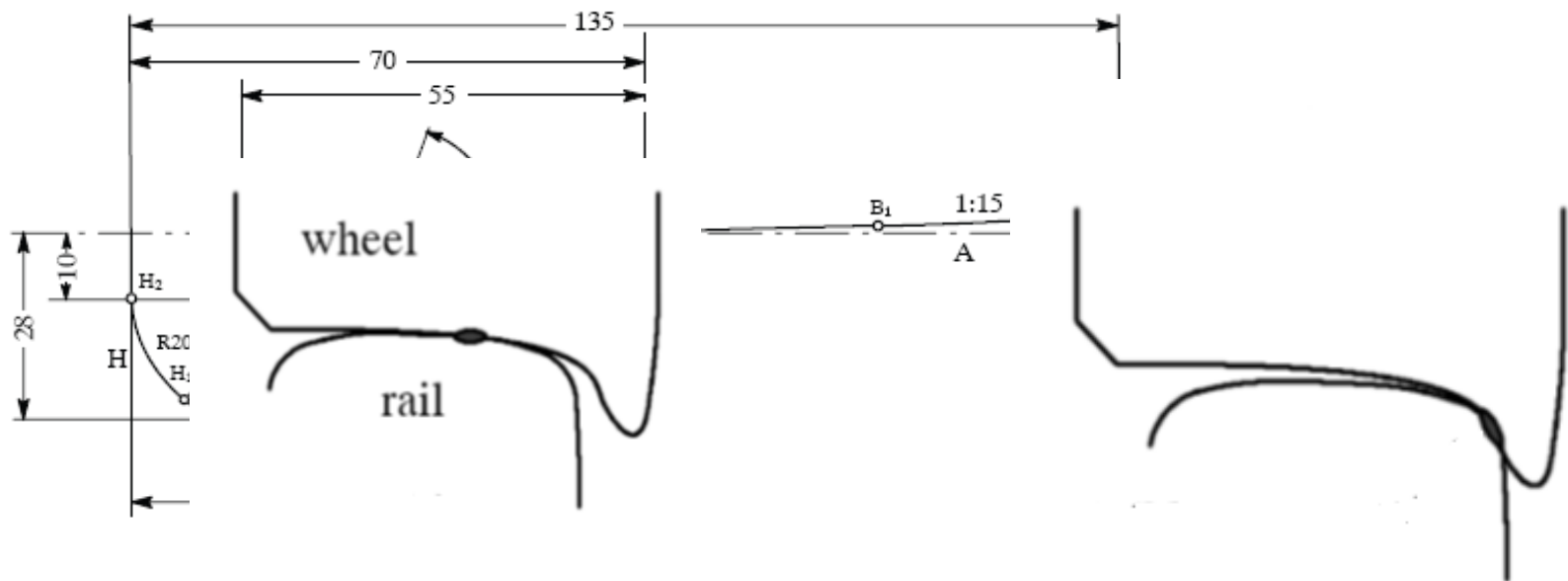
$$\alpha = -0.3 \text{ mrad}$$

$$\alpha = 7 \text{ mrad}$$



# How to solve the conflict between straight track and curving?

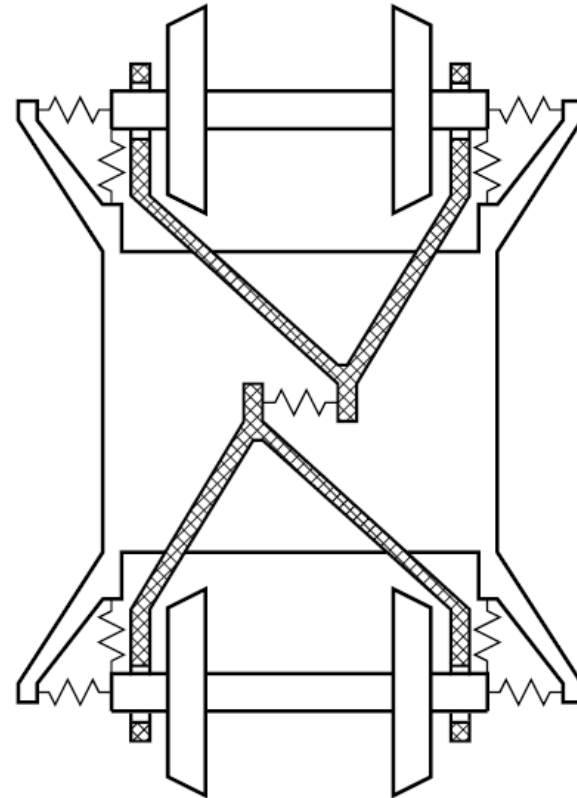
A real wheel profile is not a straight cone:



# How to solve the conflict between straight track and curving?

"Scheffel" bogie

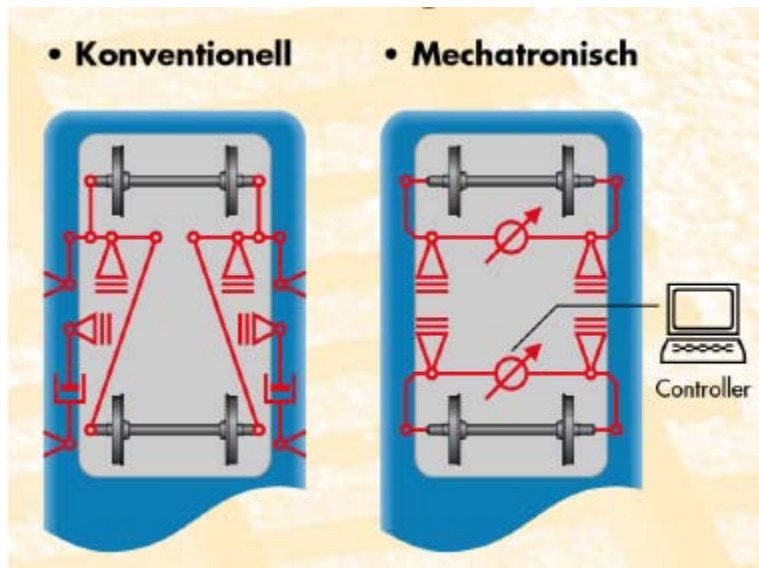
- stiff in shear
- flexible in bending





# How to solve the conflict between straight track and curving?

Active radial steering



# Another conflict...

... The design of a wheel rail profile combination

Two tasks:

- Vehicle guidance (as described before)
- Transfer loads from wheel to rail



# Contact pressure according to Hertz

Rail: UIC 60 or similar

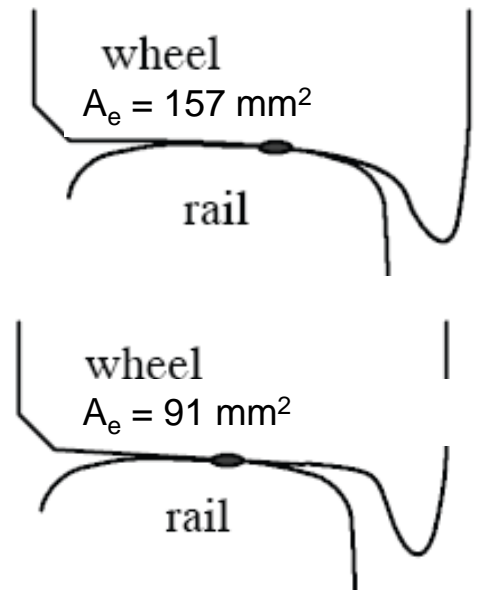
Wheel:  $r_0 = 0.46$  m ( $\varnothing$  920 mm)

Normal force  $Q = 60$  kN

Calculated contact pressure

1) Wheel UIC S1002  $\Rightarrow \sigma_{\max} = 573$  Mpa

2) Straight conical wheel  $\Rightarrow \sigma_{\max} = 990$  Mpa



Steel material is often stressed above its yield limit!

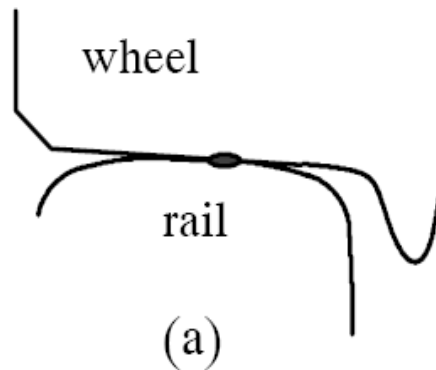


# Types of contact

Straight conical wheel profile

Wear-adapted wheel profile

no flange contact



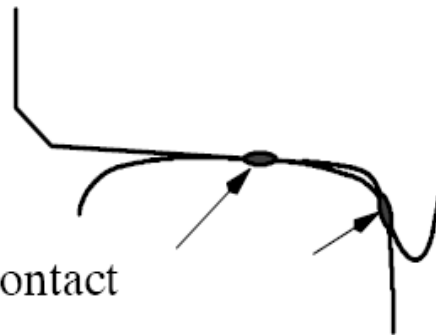
wheel

rail

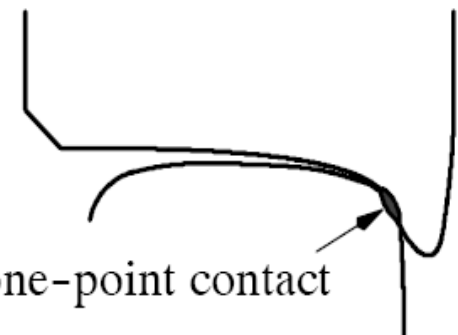
(c)

flange contact

two-point contact

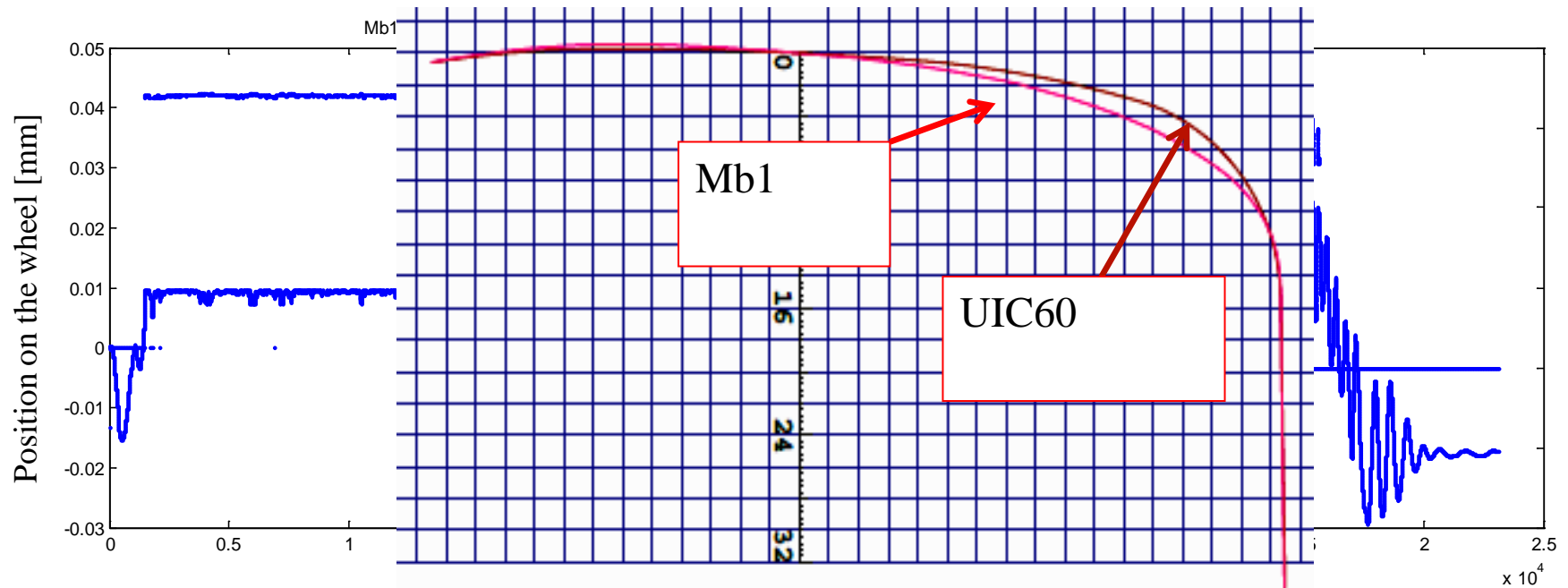


one-point contact



# Types of contact

Example iron ore line in Northern Sweden



# Types of contact

Wheel S1002  
Rail UIC 60

